Hei-Chi Chan Machin-type formulas expressing π in terms of ϕ , Fibonacci Quart. **46/47** (2008/2009), no. 1, 32–37.

Abstract

In this paper, we prove some formulas for π that are expressed in terms of the powers of the reciprocal of the Golden Ratio ϕ . These formulas depend on Machin-type identities like the following:

$$\pi = 12 \arctan\left(\frac{1}{\phi^3}\right) + 4 \arctan\left(\frac{1}{\phi^5}\right).$$