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Polynomials Defined by a Second-order Recurrence, Interlacing Zeros, and Gray Codes, Fibonacci Quart. **48** (2010), no. 3, 209–218.

Abstract

A sequence of polynomials is defined by the recurrence $P_{n+1} = (P_n + c - a)^2 - c$, with $P_0 = x - c$. Conditions are found for interlacing zeros among these polynomials, and an association between zeros and Gray codes is described. If c = a = 2, the polynomials are closely related to Chebyshev polynomials of the first kind.