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**Abstract**

We introduce an analogue of the Ducci game that involves  $d$ -tuples of prime numbers subjected to the iteration  $G$  sending such a  $d$ -tuple  $(p_1, p_2, \dots, p_d)$  into  $(\text{gpf}(p_1 + p_2), \text{gpf}(p_2 + p_3), \dots, \text{gpf}(p_d + p_1))$ , where for any  $x \geq 1$ ,  $\text{gpf}(x)$  represents the greatest prime factor of the integer  $x$ . We show that the iteration of  $G$  always leads into a limit cycle  $C$ . Moreover, if  $C$  has length greater than 1, then not only every vector in  $C$  has all components in  $P_0 := \{2, 3, 5, 7\}$ , but every element of  $P_0$  appears as a component of some vector in  $C$ . An analysis of the lengths of the nontrivial cycles for small values of  $d$  is provided.