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Abstract

We show that the generalized repunit $(b^n - 1)/(b - 1)$ is divisible by n if and only if n is divisible by the multiplicative order of b modulo every prime factor of n. This fact is a generalization of an older result which holds for b = 10. A few consequences of this theorem concerning base-b Niven numbers are also discussed.