Arthur T. Benjamin and Joel Ornstein A Bijective Proof of a Derangement Recurrence, Fibonacci Quart. **55** (2017), no. 5, 28–29.

Abstract

The number of permutations of order n with no fixed points is called the nth derangement number, and is denoted by D_n . It is well-known that for n > 1, the derangement numbers satisfy the recurrence $D_n = nD_{n-1} + (-1)^n$. We present a simple combinatorial proof of this recurrence.