# MISCELLANEOUS PROBLEM INDEX Problems by Proposer, Number, Topic & Location, & by Solution Location

**Note**: Many problems in this section are exercises or conjectures, sometimes proven in other research papers. Solutions and location of solutions, unless specifically given as solutions in *TFQ*, are not provided. Also not included are problems and projects which authors indicate that they will pursue themselves. Problems from multiple authors are listed initially by the first author listed in the article. Problem numbers (mostly) are those of the proposers.

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- 1.2 To: Two consecutive Fibonacci numbers are relatively prime 1.2(1963)59; Hint 1.2(1963)80
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