

## SUBJECT INDEX

This Index replaces the former Quick Reference Key Word Index. This Index provides sub topic listings for the larger categories . For example, generating functions has about 100 sub-listings.

Entries are listed by volume and issue number (page number) using the format **vol #.issue #(page #)** and the page reference is indicated by the **beginning** of the article in which the topic appears. Some topics have several sub categories and can be found under the specific heading. For example, most things relating to Pell such as equations, identities or polynomials are listed under Pell, not under equations, identities or polynomials, respectively. But in some cases appear under other specific headings.

Since the topic “Fibonacci” has an immense number of entries, it seemed prudent to segregate Fibonacci topics. Similarly for Lucas topics. So for the letter “F” all non-Fibonacci topic listings appear first, followed by listings “Fibonacci-A”, etc. Similarly for the letter “L” and “Lucas-A”, etc. Other topics are listed in a natural way.

Note that this Index is intended to be as complete as possible. However there are bound to be sins of omission, some intentional, some not. If you use this Index and are unable to find something, please inform the indexer at [<charliecook29150@aim.com>](mailto:charliecook29150@aim.com) so that any missing topic will be available in the next version submitted to the Fibonacci Home Page. Note that some duplication of entries exists.

Year references for each volume are as follows with the number of issues in parentheses.

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54: 2016 (4)	55: 2017 (4)	56: 2018 (4)	57: 2019 (4)
58: 2020 (4)	59: 2021 (4)	60: 2022 (4)	

MRFS: 18th Anniversary Collection of Manuscripts Related to the Fibonacci Sequence (1980)  
International Conference Proceedings (Conference date, publication dat)

PI (1984,1986) PII (1986,1988) PIII (1988,1990) PIV (1990,1991) PV (1992,1993)  
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\* No Proceedings were printed for the 2000 International Conference. So PIX refers to the 10th International Conference, etc.

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