ON FERNS' THEOREM ON THE EXPANSION OF FIBONACCI AND LUCAS NUMBERS

 $\alpha^r \ = \frac{L_r + dF_r}{2A} \ , \qquad \beta^r \ = \ \frac{L_r - dF_r}{2B}$

$$\begin{aligned} \frac{1}{2A}(L_{x_1+x_2}+\dots+x_n+dF_{x_1+x_2}+\dots+x_n) \\ &= a^{x_1+x_2}+\dots+x_n \\ &= \frac{1}{2^nA^n}(L_{x_1}+dF_{x_1})(L_{x_2}+dF_{x_2})\dots(L_{x_n}+dF_{x_n}) \\ &= \frac{1}{2^nA^n}(S_0^n+dS_1^n+d^2S_2^n+\dots+d^nS_n^n). \end{aligned}$$

Similarly

$$\frac{1}{2B} \left(L_{x_1 + x_2 + \dots + x_n} - dF_{x_1 + x_2 + \dots + x_n} \right)$$
$$= \frac{1}{2^n B^n} \left(S_0^n - dS_1^n + d^2 S_2^n - \dots + (-1)^n d^n S_n^n \right) .$$

The theorem now follows by addition and subtraction.

REFERENCES

- 1. H.H. Ferns, "Products of Fibonacci and Lucas Numbers," *The Fibonacci Quarterly*, Vol. 7, No. 1 (Feb. 1969), pp. 1–13.
- 2. A.J.W. Hilton, "On the Partition of Horadam's Generalized Sequences into Generalized Fibonacci and Lucas Sequences," *The Fibonacci Quarterly*, to appear.

THE FIBONACCI ASSOCIATION

RESEARCH CONFERENCE

PROGRAM OF SATURDAY, MAY 4, 1974

ST. MARY'S COLLEGE

| 9:00–9:30 9:30–10:15 | PRELIMINARY GATHERING, coffee and rolls. SEQUENCES GENERATED BY LEAST INTEGER FUNCTIONS Brother Alfred Brousseau, St. Mary's College |
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| 10:20-11:00 | THE SEQUENCES 1, 5, 16, 45, 121, 320, … IN COMBINATORICS Ken Rebman, California State University, Hayward |
| 11:05-11:46 | REPRESENTATION OF INTEGERS USING FIBONACCI AND LUCAS SQUARES Hardy Reyerson, Masters Student, San Jose State University |
| 12:00-1:30 | LUNCH PERIOD |
| 1:30–2:15 | RECTANGULAR AND TRIANGULAR PARTITIONS Leonard Carlitz, Duke University |
| 2:20-3:00 | GREAT ADVENTURES WITH CATALAN AND LAGRANGE Verner E. Hoggatt, Jr., San Jose State University |
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