

Since we wish $y/x > 0$, then $\alpha = (k + \sqrt{k^2 + 4})/2$ is selected. In reality, this leads naturally to the Fibonacci polynomials. Suppose again we start out with $f_0 = p$ and $f_1 = 1$, $f_2 = p - k$,

$$\begin{aligned} f_3 &= 1 - k(p - k) = k^2 - kp + 1 = (k^2 + 1) - pk \\ f_4 &= (p - k) - k(k^2 - kp + 1) = (-k^3 - 2k) + p(k^2 + 1) = -u_4(k) + pu_3(k) \\ f_n &= (-1)^n [u_{n+1}(k) - pu_n(k)], \end{aligned}$$

where $u_n(k)$ is the n^{th} Fibonacci polynomial. Once again $\lim_{n \rightarrow \infty} f_n$ does not exist unless

$$p = (k + \sqrt{k^2 + 4})/2;$$

then

$$\begin{aligned} f_n &= (-1)^n u_n(k) \left(\frac{u_{n+1}(k)}{u_n(k)} - p \right). \\ \lim_{n \rightarrow \infty} f_n &= 0 \end{aligned}$$

as before. When $k = 1$ ($u_n(1) = F_n$) so that unless $p = \alpha$, then

$$f_n = (-1)^n [u_{n+1}(k) - \alpha u_n(k) - (p - \alpha)u_n(k)] = (-1)^n \cdot 1 + (-1)^n (\alpha - p)u_n(k)$$

which diverges since $\lim_{n \rightarrow \infty} u_n(k) \rightarrow \infty$ for each $k > 0$.

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