

PROPERTIES OF SOME EXTENDED BERNOULLI AND EULER POLYNOMIALS

6. D. Foata & M. P. Schützenberger. *Théorie Géométrique des polynômes Eulériens*. Lecture Notes in Math 138. Berlin, Heidelberg, New York: Springer-Verlag, 1970.
7. B. K. Karande & N. K. Thakare. "On the Unification of Bernoulli and Euler Polynomials." *Indian J. Pure Appl. Math.* 6 (1975):98-107.
8. M. Mikolas. "Integral Formulas of Arithmetical Characteristics Relating to the Zeta-Function of Hurwitz." *Publicationes Mathematicae* 5 (1957):44-53.
9. L. J. Mordell. "Integral Formulas of Arithmetical Character." *J. London Math. Soc.* 33 (1959):371-75.

◆◆◆◆

COMMENT ON PROBLEM H-315

WILHELM WERNER

*Johannes Gutenberg-Universität in Mainz*

Recently I came to know Problem H-315 of *The Fibonacci Quarterly* (Vol. 18, 1980) which deals with "Kerner's method" for the simultaneous determination of polynomial roots. I want to comment on two aspects of the problem and its solution.

1. The method was already used by K. Weierstrass for a constructive proof of the fundamental theorem of algebra (cf. [1]). Kerner [2] realized that the method can be interpreted as a Newton method for the elementary symmetric functions; this fact is also observed in the textbook of Durand ([3], pp. 279-80) which appeared several years before Kerner's publication.

2. It is remarkable that the assumption

$$\sum_{i=1}^n z_i = -a_{n-1}$$

is *not* necessary for the validity of the assertion! This fact is mentioned by Byrnev and Dochev [4] where further references are given. The proof of the assertion

$$\sum_{i=1}^n \hat{z}_i = -a_{n-1}$$

is easy: following Kerner's derivation of the method, one must apply Newton's method to the system of elementary symmetric functions. Hence, one of the equations reads:

$$\sum_{i=1}^n x_i = -a_{n-1} \quad (x_1, x_2, \dots, x_n \text{ denote the unknowns}).$$

[Please turn to page 188]