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CONTENTS

Expansion of the Fibonacci Numbers F_{mn+r} in the m Powers	
of Fibonacci or Lucas Numbers James E. Desmond	194
Some Combinational Sequences Joseph W. Creely	209
Hypersurfaces Associated with Simson	
Formula Analogues A. F. Horadam	221
Determinantal Hypersurfaces for Lucas Sequences of Order r , and a Generalization	227
On the Occurrences of Fibonacci Sequences in the Counting of Matchings in Linear Polygonal Chains E. J. Farrell	238
The Fibonacci Ratio in a Thermodynamical Problem: A Combinatorial Approach	247
A Further Note on Pascal Graphs B. P. Sinha, S. Ghose, B. B. Bhattacharya, & P. K. Srimani	251
On Fibonacci k-ary Trees Derek K. Chang	258
Fibonacci Numbers as Expected Values	
in a Game of Chance	263
Sequences Generated by Multiple Reflections Ian Bruce	268
A Relation for the Prime Distribution Function Paul S. Bruckman	273
Elementary Problems and	
Solutions Edited by A. P. Hillman, Gloria C. Padilla, & Charles R. Wall	277
Advanced Problems and	
Solutions Edited by Raymond E. Whitney	283

PURPOSE

The primary function of **THE FIBONACCI QUARTERLY** is to serve as a focal point for widespread interest in the Fibonacci and related numbers, especially with respect to new results, research proposals, challenging problems, and innovative proofs of old ideas.

EDITORIAL POLICY

THE FIBONACCI QUARTERLY seeks articles that are intelligible yet stimulating to its readers, most of whom are university teachers and students. These articles should be lively and well motivated, with new ideas that develop enthusiasm for number sequences or the exploration of number facts. Illustrations and tables should be wisely used to clarify the ideas of the manuscript. Unanswered questions are encouraged, and a complete list of references is absolutely necessary.

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Authors are encouraged to keep a copy of their manuscripts for their own files as protection against loss. The editor will give immediate acknowledgment of all manuscripts received.

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