

THE OFFICIAL JOURNAL OF THE FIBONACCI ASSOCIATION

## **TABLE OF CONTENTS**

Hofstadter's Extraction Conjecture	98
An Unexpected Encounter with the Fibonacci Numbers	108
Addendum to "Second Derivative Sequences of Fibonacci and Lucas Polynomials"Piero Filipponi and Alwyn F. Horadam	110
The Fibonacci and Lucas Triangles Modulo 2Diana L. Wells	111
Modified Numerical Triangle and the Fibonacci Sequence	124
Integration and Derivative Sequences for Pell and Pell-Lucas Polynomials	130
The Order of a Perfect k-ShuffleRobert W. Packard and Erik S. Packard	136
Book Announcement: Generalized Pascal Triangles and Pyramids: Their Fractals, Graphs, and Applicationsby Dr. Boris A. Bondarenko	144
On Some Properties of Fibonacci Diagonals in Pascal's Triangle	145
Fifth International Conference Proceedings	152
On the Infinitude of Lucas PseudoprimesPaul S. Bruckman	153
Lucas Pseudoprimes are OddPaul S. Bruckman	155
On a Conjecture of Di Porto and FilipponiPaul S. Bruckman	158
Extensions to the GCD Star of David Theorem	160
Author and Title Index for Sale	166
Fibonacci Numbers and a Chaotic Piecewise Linear FunctionJ.S. Frame	167
Generating Solutions for a Special Class of Diophantine EquationsPasquale J. Arpaia	170
Sequences of Consecutive <i>n</i> -Niven Numbers	174
A Bracket Function Transform and Its Inverse	176
Elementary Problems and SolutionsEdited by Stanley Rabinowitz	180
Advanced Problems and Solutions	187

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#### PURPOSE

The primary function of **THE FIBONACCI QUARTERLY** is to serve as a focal point for widespread interest in the Fibonacci and related numbers, especially with respect to new results, research proposals, challenging problems, and innovative proofs of old ideas.

### EDITORIAL POLICY

**THE FIBONACCI QUARTERLY** seeks articles that are intelligible yet stimulating to its readers, most of whom are university teachers and students. These articles should be lively and well motivated, with new ideas that develop enthusiasm for number sequences or the exploration of number facts. Illustrations and tables should be wisely used to clarify the ideas of the manuscript. Unanswered questions are encouraged, and a complete list of references is absolutely necessary.

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# The Fibonacci Quarterly

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