



The Fibonacci Quarterly

THE OFFICIAL JOURNAL OF THE FIBONACCI ASSOCIATION

TABLE OF CONTENTS

On p -adic Complementary Theorems between Pascal's Triangle and the Modified Pascal Triangle	<i>Shiro Ando and Daihachiro Sato</i>	194
A Number Theoretic Function Arising from Continued Fractions	<i>H.C. Williams</i>	201
Uniqueness of Representations by Morgan-Voyce Numbers	<i>A.F. Horadam</i>	212
Announcement of the Ninth International Conference on Fibonacci Numbers and Their Applications		216
Obtaining New Dividing Formulas $n Q(n)$ from the Known Ones	<i>Bau-Sen Du</i>	217
On the Fibonacci Numbers and the Dedekind Sums	<i>Zhang Wenpeng and Yi Yuan</i>	223
Residues of Generalized Binomial Coefficients Modulo a Prime	<i>John M. Holte</i>	227
Generalized Jacobsthal Polynomials	<i>Gospava B. Djordjević</i>	239
Conditions for the Existence of Generalized Fibonacci Primitive Roots	<i>Hua-Chieh Li</i>	244
Families of Solutions of a Cubic Diophantine Equation	<i>Marc Chamberland</i>	250
New Problem Website		253
Alternating Sums of Fourth Powers of Fibonacci and Lucas Numbers	<i>R.S. Melham</i>	254
Author and Title Index		259
Completion of Numerical Values of Generalized Morgan-Voyce and Related Polynomials	<i>A.F. Horadam</i>	260
A Remark on Parity Sequences	<i>James H. Schmerl</i>	264
New Elementary Problems and Solutions Editors		271
Complete and Reduced Residue Systems of Second-Order Recurrences Modulo p	<i>Hua-Chieh Li</i>	272
Phased Tilings and Generalized Fibonacci Identities	<i>Arthur T. Benjamin, Jennifer J. Quinn, and Francis Edward Su</i>	282

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PURPOSE

The primary function of **THE FIBONACCI QUARTERLY** is to serve as a focal point for widespread interest in the Fibonacci and related numbers, especially with respect to new results, research proposals, challenging problems, and innovative proofs of old ideas.

EDITORIAL POLICY

THE FIBONACCI QUARTERLY seeks articles that are intelligible yet stimulating to its readers, most of whom are university teachers and students. These articles should be lively and well motivated, with new ideas that develop enthusiasm for number sequences or the exploration of number facts. Illustrations and tables should be wisely used to clarify the ideas of the manuscript. Unanswered questions are encouraged, and a complete list of references is absolutely necessary.

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Articles should be submitted using the format of articles in any current issues of **THE FIBONACCI QUARTERLY**. They should be typewritten or reproduced typewritten copies, that are clearly readable, double spaced with wide margins and on only one side of the paper. The full name and address of the author must appear at the beginning of the paper directly under the title. Illustrations should be carefully drawn in India ink on separate sheets of bond paper or vellum, approximately twice the size they are to appear in print. Since the Fibonacci Association has adopted $F_1 = F_2 = 1$, $F_n + 1 = F_n + F_{n-1}$, $n \geq 2$ and $L_1 = 1$, $L_2 = 3$, $L_n + 1 = L_n + L_{n-1}$, $n \geq 2$ as the standard definitions for The Fibonacci and Lucas sequences, these definitions *should not* be a part of future papers. However, the notations *must* be used. One to three *complete* A.M.S. classification numbers *must* be given directly after references or on the bottom of the last page. **Papers not satisfying all of these criteria will be returned.** See the new worldwide web page at:

<http://www.sdstate.edu/~wsc/http/fibhome.html>

for additional instructions.

Two copies of the manuscript should be submitted to: **CURTIS COOPER, DEPARTMENT OF MATHEMATICS AND COMPUTER SCIENCE, CENTRAL MISSOURI STATE UNIVERSITY, WARRENSBURG, MO 64093-5045.**

Authors are encouraged to keep a copy of their manuscripts for their own files as protection against loss. The editor will give immediate acknowledgment of all manuscripts received.

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DEVOTED TO THE STUDY
OF INTEGERS WITH SPECIAL PROPERTIES

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PROFESSOR CURTIS COOPER, Department of Mathematics and Computer Science, Central Missouri State University, Warrensburg, MO 64093-5045 e-mail: cnc8851@cmsu2.cmsu.edu

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