

There are two other results of interest. First, we have a somewhat similar relation between  $S_{4r}$  and  $F_{2r+2}$ , namely

$$S_{4r} = c_{2r} F_{2r+2} - 2b .$$

This can easily be proved in the same way as the earlier result.

Second, it follows from the earlier results that

$$S_n = F_{n+2} - b ,$$

and hence that

$$S_{n+2} = S_n + S_{n+1} + b .$$



[Continued from page 295.]

— for (5<sup>bis</sup>), the product  $AB$  by the product of the values of  $A$  and  $B$  relative to the sequences  $y$  and  $z$ , and, on the other hand,  $\phi$  by the sum of the values of  $\phi$  for these sequences.

— for (6<sup>bis</sup>)  $\sqrt{AB}$  by  $AB$  and  $\phi$  by  $2\phi$ ,

— for (7<sup>bis</sup>)  $\sqrt{AB}$  by  $AB$  and  $\phi$  by  $p + 2\phi$ .

12. The author thinks he has shown, by the present study which does not maintain to be exhaustive, how much the use of hyperbolic lines to express the terms of the linear sequences of the type (1) is favorable by the simplicity which it introduces in the calculations bearing on these sequences, by the fact also that it suggests relations, which makes it easier to set up. These advantages are specially clear in the case of the Fibonacci and Lucas sequences, for which it is possible to re-establish quickly the well known formulas concerning them.

